Name $\qquad$
$\qquad$
INSTRUCTIONS: You must show enough work to justify your answer on ALL problems. Correct answers with no work (or inconsistent work) shown will not receive full credit. All answers are to be exact; no decimal approximations. You are NOT allowed to use any electronic device for this exam.

1. Sketch the graph of the following functions. Label at most three number(s) on the $x$-axis and/or $y$-axis to help identify your sketch. Then state the domain and range of the function in interval notation. (14 pts.)
a. $\quad f(x)=2\left(\frac{5}{7}\right)^{x}-6$
b. $\quad g(x)=\log _{2}(x+3)+4$


Domain $\qquad$ Range $\qquad$ Domain $\qquad$ Range $\qquad$
2. Use the properties of logarithms to write the following as a sum and/or difference of logarithms. All variables represent positive numbers. (7 pts.) Put a box around your answer.
$\ln \frac{x^{2}\left(x^{2}+4\right)^{5}}{(x-6) \sqrt[3]{5-3 x}}$
3. Write $\log (2 x+7)-5 \log \left(x^{4}-16\right)+\frac{3}{4} \log \left(x^{3}+8\right)$ as a single logarithm. (6 pts.) Put a box around your answer.
4. Use the change of basis formula to write $\log _{5} 35$ in terms of base 8. (3 pts.)

Answer $\qquad$
5. Solve the following equations.
a. $\quad 9^{6 x+11}=\frac{1}{27} \quad(6$ pts. $)$

Answer $\qquad$
b. $\quad 5^{x-3}=8 \quad(7 \mathrm{pts}$.

Answer $\qquad$
c. $\quad \log _{3} x=2+\log _{3}(x+4) \quad(8$ pts. $)$

Answer $\qquad$
6. Solve the following systems of equations by the indicated method.
a. $\quad \begin{aligned}-2 x+3 y & =-8 \\ 5 x+6 y & =2\end{aligned}$ using the addition method ( 6 pts.)

Answer $\qquad$
b.

$$
\begin{aligned}
3 x+7 y & =26 \\
x+4 y & =17
\end{aligned} \quad \text { using the substitution method } \quad(7 \mathrm{pts} .)
$$

Answer $\qquad$
c. $\quad \begin{aligned} x^{2}+y^{2} & =9 \\ 2 x-y & =-3\end{aligned}$ using the substitution method ( 9 pts.)

Answer $\qquad$
7. Determine the solution for the system represented by each augmented matrix. (10 pts.)
a. $\quad\left[\begin{array}{ccc|c}2 & -3 & 6 & -5 \\ 0 & 1 & 4 & 7 \\ 0 & 0 & 0 & 0\end{array}\right]$
b. $\quad\left[\begin{array}{ccc|c}4 & -7 & 9 & -6 \\ 0 & 1 & -8 & 12 \\ 0 & 0 & 0 & -3\end{array}\right]$

Answer $\qquad$ Answer $\qquad$
8. Solve the following system of equations using Gaussian elimination. Indicate your row operations. (12 pts.)

$$
\begin{aligned}
x-2 y+5 z & =11 \\
3 x-4 y-2 z & =-16 \\
-2 x+5 y-6 z & =-9
\end{aligned}
$$

$\qquad$

